

Cambridge IGCSE™

ADDITIONAL MATHEMATICS**0606/21**

Paper 2

October/November 2024

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1	$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$	M1	
	$\frac{\sin^2 \theta + \cos^2 \theta}{\cos \theta \sin \theta}$	A1	
	$\frac{1}{\cos \theta \sin \theta}$ oe and completion to given answer $\sec \theta \operatorname{cosec} \theta$	A1	
	Alternative		
	$\left[\tan \theta + \frac{1}{\tan \theta} \right] = \frac{\tan^2 \theta + 1}{\tan \theta}$	(M1)	
	$\frac{\sec^2 \theta}{\tan \theta}$	(A1)	
	$\frac{\sec^2 \theta \cos \theta}{\sin \theta}$ oe and completion to given answer $\sec \theta \operatorname{cosec} \theta$	(A1)	
2(a)	$\left[\frac{dy}{dx} = \right] \tan^2 x$ nfw	B2	B1 for $\sec^2 x - 1$
2(b)	$\left[\tan x - x \right]_0^{\frac{\pi}{4}}$	M1	
	$1 - \frac{\pi}{4}$ or exact equivalent	A1	
3(a)	$\left(8^x \right)^2 - 8^x - 2$ [= 0] oe or $\left(2^{\frac{3}{x}} \right)^2 - 2^{\frac{3}{x}} - 2$ [= 0] oe	B1	
	$(8^{\frac{1}{x}} - 2)(8^{\frac{1}{x}} + 1) = 0$ oe or $(2^{\frac{3}{x}} - 2)(2^{\frac{3}{x}} + 1) = 0$ oe	M1	FT their 3-term quadratic in $8^{\frac{1}{x}}$ oe
	$8^{\frac{1}{x}} = 2$ $\left[8^{\frac{1}{x}} = -1 \right]$ or $2^{\frac{3}{x}} = 2$ $\left[2^{\frac{3}{x}} = -1 \right]$ oe	A1	
	$x = 3$ nfw	A1	

Question	Answer	Marks	Partial Marks
3(b)	$a^2 - 2\sqrt{3}a + 3 [= b + (3 - b)\sqrt{3}]$	B1	
	Equates coefficients to form two equations	M1	FT their $(a^2 - 2\sqrt{3}a + 3) = b + (3 - b)\sqrt{3}$ providing of equivalent difficulty
	$a^2 + 3 = b$ and $-2a = 3 - b$ oe	DM1	FT their $(a^2 - 2\sqrt{3}a + 3) = b + (3 - b)\sqrt{3}$
	$a^2 - 2a [= 0]$ or $b^2 - 10b + 21 [= 0]$	DM1	
	$a = 2, 0$ or $b = 3$ or 7	A1	
	$a = 2, b = 7$ and $a = 0, b = 3$	A1	
4	$\mathbf{b - a = \frac{p}{p+q} (c - a)}$ oe AND Correct completion to given answer $\mathbf{b = \frac{qa + p c}{q + p}}$	5	B4 for $\mathbf{b - a = \frac{p}{p+q} (c - a)}$ OR B1 for $\overrightarrow{AB} = \frac{p}{p+q} \overrightarrow{AC}$ soi B1 for $\overrightarrow{AB} = \mathbf{b - a}$ soi B1 for $\overrightarrow{AC} = \mathbf{c - a}$ soi
	Alternative 1		
	$q(\mathbf{b - a}) = p(\mathbf{c - b})$ oe AND Correct completion to given answer $\mathbf{b = \frac{qa + p c}{q + p}}$	(5)	B4 for $q(\mathbf{b - a}) = p(\mathbf{c - b})$ OR B1 for $q \overrightarrow{AB} = p \overrightarrow{BC}$ soi B1 for $\overrightarrow{AB} = \mathbf{b - a}$ soi B1 for $\overrightarrow{BC} = \mathbf{c - b}$ soi
	Alternative 2		
	$\mathbf{b = a + \frac{p}{p+q} (c - a)}$ oe or $\mathbf{b = c + \frac{q}{p+q} (a - c)}$ oe AND Correct completion to given answer $\mathbf{b = \frac{qa + p c}{q + p}}$	(5)	B4 for $\mathbf{b = a + \frac{p}{p+q} (c - a)}$ oe or $\mathbf{b = c + \frac{q}{p+q} (a - c)}$ oe OR B1 for $\overrightarrow{OB} = \overrightarrow{OA} + \overrightarrow{AB}$ or $\overrightarrow{OB} = \overrightarrow{OC} + \overrightarrow{CB}$ soi B1 for $\overrightarrow{AB} = \frac{p}{p+q} \overrightarrow{AC}$ or $\overrightarrow{CB} = \frac{q}{p+q} \overrightarrow{CA}$ soi B1 for $\overrightarrow{AC} = \mathbf{c - a}$ or $\overrightarrow{CA} = \mathbf{a - c}$ soi

Question	Answer	Marks	Partial Marks
5	$\log_a \left(\frac{5(p+1)p}{p+2} \right) = \log_a 12$ oe, nfw or $\frac{5(p+1)p}{p+2} = 12$ oe, nfw	M2	M1 for correct use of one log law in a correct equation e.g. $\log_a(p+1) + \log_a p - \log_a(p+2)$ $+ \log_a 5 = \log_a 12$ or $\log_a p(p+1) - \log_a(p+2)$ $= \log_a 12 - \log_a 5$ or $\log_a \frac{p+1}{p+2} + \frac{1}{\log_p a}$ $+ \log_a 5 = \log_a 12$
	$5p^2 - 7p - 24 = 0$	A1	
	$(5p+8)(p-3) = 0$ or formula	DM1	FT their 3-term quadratic
	$p = 3$ and no other solution nfw	A1	
6(a)	OA: $2\sqrt{3}$ or $\sqrt{12}$ soi	B1	
	Correct method to find angle AOE e.g. $2\tan(\dots) = \frac{3}{\sqrt{3}}$ oe or $36 = 12 + 12 - 2(12)\cos AOE$ oe or $\pi - 2\tan^{-1} \frac{\sqrt{3}}{3}$ oe	M1	
	Angle AOE: $\frac{2\pi}{3}$ soi, isw	A1	
	Arc AFE: their $2\sqrt{3} \times \text{their } \frac{2\pi}{3}$ soi or $\frac{4\sqrt{3}}{3}\pi$	M1	FT their $\frac{2\pi}{3}$ and their $2\sqrt{3}$
	Perimeter: $10 + 2\sqrt{3} + \frac{4\sqrt{3}}{3}\pi$ or exact equivalent, cao	A1	

Question	Answer	Marks	Partial Marks
6(b)	Sum of three correct areas $4\pi + 12 + 3\sqrt{3}$ cao	3	M2 FT their $\frac{2\pi}{3}$ and their $2\sqrt{3}$ for sector AOE: $\frac{1}{2} \times (\text{their } 2\sqrt{3})^2 \times \text{their } \frac{2\pi}{3}$ oe or 4π and $\frac{1}{2} \times 6 \times 4$ or $2 \times \frac{1}{2} \times 3 \times \sqrt{3}$ oe or M1 FT their $\frac{2\pi}{3}$ and their $2\sqrt{3}$ for sector AOE: $\frac{1}{2} \times (\text{their } 2\sqrt{3})^2 \times \text{their } \frac{2\pi}{3}$ oe or 4π
7	Attempts product rule	M1	
	$\frac{dy}{dx} = 2\cos x - 2x\sin x$ oe	A1	
	When $x = \pi$, $\frac{dy}{dx} = -2$	DM1	FT their $\frac{dy}{dx} \Big _{x=\pi}$
	Gradient of normal: $\frac{1}{2}$	M1	FT $\frac{-1}{\text{their } \frac{dy}{dx} \Big _{x=\pi}}$
	$y + 2\pi = \frac{1}{2}(x - \pi)$ oe	A1	FT their normal gradient
	$(5\pi, 0)$ or $(0, -\frac{5}{2}\pi)$ oe, soi	A1	
	Area of triangle POQ: $\frac{25}{4}\pi^2$ nfww	A1	
8(a)	$3t^2 + 2t - 1$	B1	
	$(3t - 1)(t + 1)$	M1	FT their 3-term quadratic in $t = 0$ soi
	$t = \frac{1}{3}$ and no other solutions	A1	
8(b)	At $t = 0$, $x = 8$ and $v = -1$	B2	B1 for $t = 0$, $x = 8$ or $t = 0$, $v = -1$
	Conclusion: Since x is positive and v is negative [the particle is moving towards O.]	B1	

Question	Answer	Marks	Partial Marks
8(c)	$t = \frac{1}{3} \times \frac{211}{27}$ or 7.814[814...] rot to 4 or more sf	B1	
	Distance $t = 0$ to $t = \frac{1}{3}$: $8 - \frac{211}{27}$ or $\frac{5}{27}$ or 0.1851[85...] rot to 4 or more sf and Distance $t = \frac{1}{3}$ to $t = 2$: $18 - \frac{211}{27}$ or $\frac{275}{27}$ or 10.18[51...] rot to 4 or more sf	M2	M1 for distance $t = 0$ to $t = \frac{1}{3}$: $8 - \frac{211}{27}$ or $\frac{5}{27}$ or 0.1851[85...] rot to 4 or more sf or $t = \frac{1}{3}$ to $t = 2$: $18 - \frac{211}{27}$ or $\frac{275}{27}$ or 10.18[51...] rot to 4 or more sf
	Total: 10.4 or 10.37[037...] rot to 4 or more sf	A1	
9(a)(i)	$c = 12$	B1	
9(a)(ii)	$\frac{dy}{dx} = 2x - 8 = 0$ or $x^2 - 8x + c = (x - 4)^2 - 16 + c$	M1	
	$3 = -16 + c$ or $3 = 4^2 - 8 \times 4 + c$	DM1	
	$c = 19$	A1	
9(b)	$c > 16$	B2	B1 for $c * 16$ where * is = or an incorrect inequality sign
10(a)	${}^7C_3 \times {}^8C_3 + {}^7C_4 \times {}^8C_2$	M2	M1 for ${}^7C_3 \times {}^8C_3$ or ${}^7C_4 \times {}^8C_2$
	2940	A1	
10(b)	${}^6P_4 \times 3 \times 5$ oe	M2	M1 for ${}^6P_4 [\times 1]$ or ${}^6P_4 \times 3$ or ${}^6P_4 \times 5$ oe
	5400	A1	
11(a)(i)	Valid explanation e.g. The line $x = k$, where $-10 \leq k \leq 10$ cuts the curve in one point only	B1	
11(a)(ii)	$\frac{\frac{x}{x-1}}{\frac{x}{x-1}-1}$	M1	
	Correct simplification to x	A1	

Question	Answer	Marks	Partial Marks
11(a)(iii)	Valid explanation e.g. f and f^{-1} are the same or f is self-inverse oe	B1	
11(a)(iv)	Valid explanation e.g. The curve is symmetrical about line $y = x$	B1	
11(b)	$1 < g \leq 2$	B1	
11(c)	$x \neq -\frac{1}{3}$	B1	
12(a)	$d_A = 3$ and $d_B = -3$	B2	B1 for $d_A = 3$ or $d_B = -3$
	$a_n = 1 + (n-1) \times 3$ oe, isw or $a_n = 3n - 2$	B1	
	$b_n = 298 + (n-1) \times (-3)$ oe, isw or $b_n = -3n + 301$	B1	
	Solves $3n - 2 - (-3n + 301) = 45$ oe to find a value of n	M1	FT their $a_n - (-3n + 301)$ or $3n - 2$ – their b_n
	$n = 58$	A1	
12(b)	$3m - 2 * 2(-3m + 301)$ oe where * is = or any inequality sign	M1	FT their a_n and their b_n from part (a)
	$m * 67.1[11\dots]$ where * is = or any inequality sign	A1	
	68	A1	