



CANDIDATE  
NAME

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CENTRE  
NUMBER

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9231/32

May/June 2022

**1 hour 30 minutes**

You must answer on the question paper.

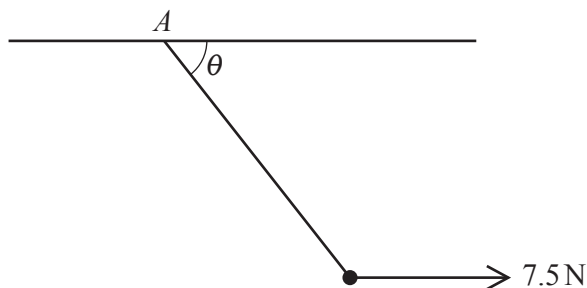
You will need: List of formulae (MF19)

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10\text{ ms}^{-2}$ .

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.

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(a) Find the tension in the string. [2]

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[illegible]

- 2 One end of a light inextensible string of length  $a$  is attached to a fixed point  $O$ . A particle of mass  $m$  is attached to the other end of the string. The particle is held at the point  $A$  with the string taut. The angle between  $OA$  and the downward vertical is equal to  $\alpha$ , where  $\cos \alpha = \frac{4}{5}$ . The particle is projected from  $A$ , perpendicular to the string in an upwards direction, with a speed  $\sqrt{3ga}$ . It then moves along a circular path in a vertical plane. The string first goes slack when it makes an angle  $\theta$  with the upward vertical through  $O$ .

Find the value of  $\cos \theta$ .

[5]

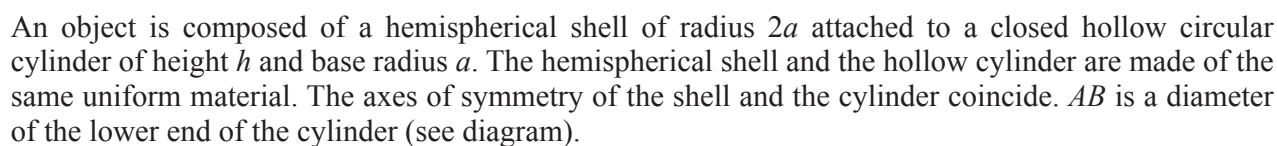
[illegible]

- 3 A particle  $P$  is moving in a horizontal straight line. Initially  $P$  is at the point  $O$  on the line and is moving with velocity  $25 \text{ m s}^{-1}$ . At time  $t \text{ s}$  after passing through  $O$ , the acceleration of  $P$  is  $\frac{4000}{(5t+4)^3} \text{ m s}^{-2}$  in the direction  $PO$ . The displacement of  $P$  from  $O$  at time  $t$  is  $x \text{ m}$ .

Find an expression for  $x$  in terms of  $t$ .

[5]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

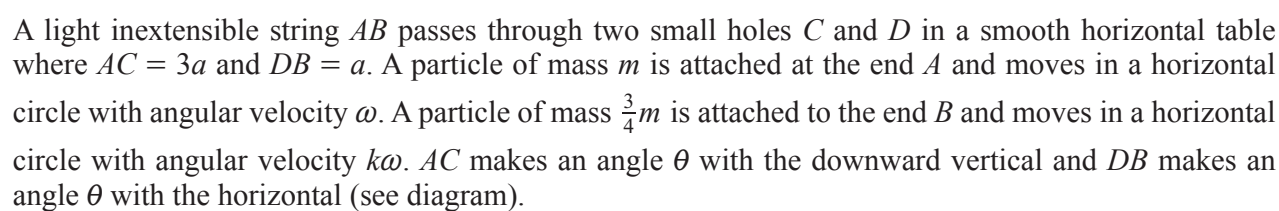


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- This image shows a full page of white paper with horizontal dashed lines, typical of primary-ruled notebook paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings present.

The object is placed on a rough plane which is inclined to the horizontal at an angle  $\theta$ , where  $\tan \theta = \frac{2}{3}$ . The object is in equilibrium with  $AB$  in contact with the plane and lying along a line of greatest slope of the plane.

**(b)** Find the set of possible values of  $h$ , in terms of  $a$ . [4]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting or typing. There are no margins, text, or other markings on the page.



[7]

[illegible]



- 6** Two uniform smooth spheres  $A$  and  $B$  of equal radii have masses  $m$  and  $km$  respectively. The two spheres are on a horizontal surface. Sphere  $A$  is travelling with speed  $u$  towards sphere  $B$  which is at rest. The spheres collide. Immediately before the collision, the direction of motion of  $A$  makes an angle  $\alpha$  with the line of centres. The coefficient of restitution between the spheres is  $\frac{1}{2}$ .
- (a)** Show that the speed of  $B$  after the collision is  $\frac{3u \cos \alpha}{2(1+k)}$  and find also an expression for the speed of  $A$  along the line of centres after the collision, in terms of  $k$ ,  $u$  and  $\alpha$ . [4]

[illegible]

After the collision, the kinetic energy of  $A$  is equal to the kinetic energy of  $B$ .

**(b)** Given that  $\tan \alpha = \frac{2}{3}$ , find the possible values of  $k$ . [5]

[illegible]

- (a) Write down expressions, in terms of  $T$ , for the horizontal displacements of  $P$  and  $Q$  from  $O$  when they collide and hence show that  $4uT = 21\sqrt{5}(T+1)$ . [4]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, leaving ample room for writing practice. There is no text or other markings on the page.

(b) Find the value of  $T$ .

[4]

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(c) Find the horizontal and vertical displacements of the particles from  $O$  when they collide.

[3]

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[illegible]



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