



CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
NUMBER

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9231/33

May/June 2022

1 hour 30 minutes

You will need: List of formulae (MF19)

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 ms^{-2} .

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.

- 1** A uniform lamina $OABC$ is a trapezium whose vertices can be represented by coordinates in the x - y plane. The coordinates of the vertices are $O(0, 0)$, $A(15, 0)$, $B(9, 4)$ and $C(3, 4)$.

Find the x -coordinate of the centre of mass of the lamina.

[4]

[illegible]

- 2 A particle P of mass m is attached to one end of a light elastic string of natural length a and modulus of elasticity $\frac{4}{3}mg$. The other end of the string is attached to a fixed point O on a rough horizontal surface. The particle is at rest on the surface with the string at its natural length. The coefficient of friction between P and the surface is $\frac{1}{3}$. The particle is projected along the surface in the direction OP with a speed of $\frac{1}{2}\sqrt{ga}$.

Find the greatest extension of the string during the subsequent motion.

[5]

[illegible]

- 3** A particle P is projected with speed 25 ms^{-1} at an angle θ above the horizontal from a point O on a horizontal plane and moves freely under gravity. After 2 s the speed of P is 15 ms^{-1} .

(a) Find the value of $\sin \theta$.

[5]

[illegible]

(b) Find the range of the flight.

[3]

[illegible]

- 4 One end of a light inextensible string of length a is attached to a fixed point O . A particle of mass m is attached to the other end of the string and is held with the string taut at the point A . At A the string makes an angle θ with the upward vertical through O . The particle is projected perpendicular to the string in a downward direction from A with a speed u . It moves along a circular path in the vertical plane.

When the string makes an angle α with the downward vertical through O , the speed of the particle is $2u$ and the magnitude of the tension in the string is 10 times its magnitude at A .

It is given that $u = \sqrt{\frac{2}{3}ga}$.

- (a) Find, in terms of m and g , the magnitude of the tension in the string at A . [6]

[illegible]

(b) Find the value of $\cos \alpha$.

[2]

- 5 A particle P of mass 4 kg is moving in a horizontal straight line. At time $t\text{ s}$ the velocity of P is $v\text{ ms}^{-1}$ and the displacement of P from a fixed point O on the line is $x\text{ m}$. The only force acting on P is a resistive force of magnitude $(4e^{-x} + 12)e^{-x}\text{ N}$. When $t = 0$, $x = 0$ and $v = 4$.

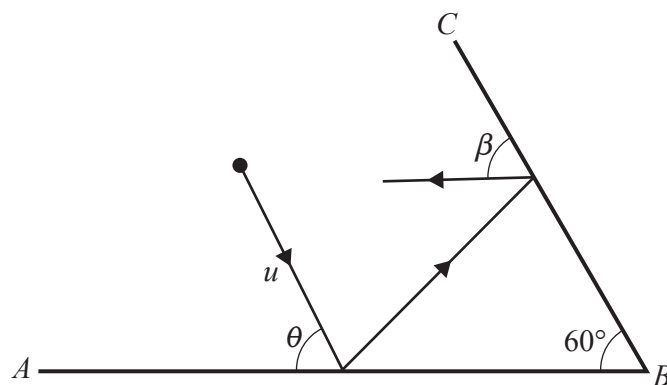
(a) Show by integration that $v = \frac{1+3e^x}{e^x}$. [4]

[illegible]

(b) Find an expression for x in terms of t .

[4]

[illegible]

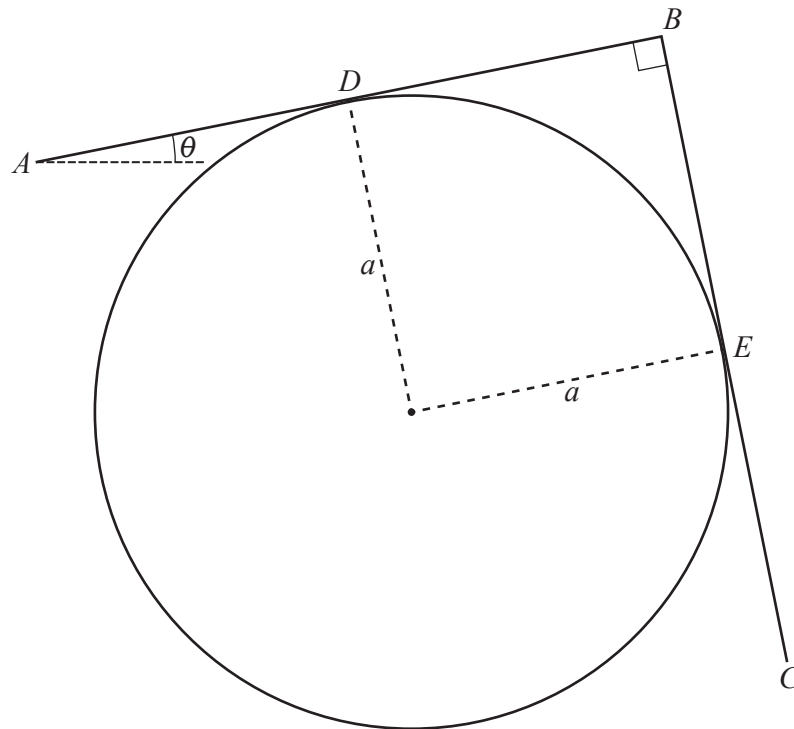


The kinetic energy of the particle after the first collision is 40% of its kinetic energy before the first collision.

- (a) Find the value of e . [4]

[illegible]

[Turn over



A uniform cylinder with a rough surface and of radius a is fixed with its axis horizontal. Two identical uniform rods AB and BC , each of weight W and length $2a$, are rigidly joined at B with AB perpendicular to BC . The rods rest on the cylinder in a vertical plane perpendicular to the axis of the cylinder with AB at an angle θ to the horizontal. D and E are the midpoints of AB and BC respectively and also the points of contact of the rods with the cylinder (see diagram). The rods are about to slip in a clockwise direction. The coefficient of friction between each rod and the cylinder is μ .

The normal reaction between AB and the cylinder is R and the normal reaction between BC and the cylinder is N .

- (a) Find the ratio $R : N$ in terms of μ . [6]

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(b) Given that $\mu = \frac{1}{3}$, find the value of $\tan \theta$. [3]

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