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## 9231/32

October/November 2022

**1 hour 30 minutes**

You will need: List of formulae (MF19)

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10\text{ ms}^{-2}$ .

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

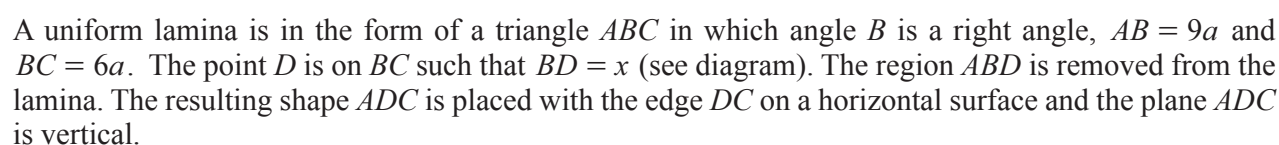
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**[Turn over**

- 1** A particle  $P$  of mass  $m$  is attached to one end of a light inextensible string of length  $a$ . The other end of the string is attached to a fixed point  $O$ . The string is held taut with  $OP$  making an angle  $\alpha$  with the downward vertical, where  $\cos \alpha = \frac{2}{3}$ . The particle  $P$  is projected perpendicular to  $OP$  in an upwards direction with speed  $\sqrt{3ag}$ . It then starts to move along a circular path in a vertical plane.

Find the cosine of the angle between the string and the upward vertical when the string first becomes slack. [4]

[illegible]

[illegible]

- 3** One end of a light elastic string, of natural length  $a$  and modulus of elasticity  $\frac{16}{3}Mg$ , is attached to a fixed point  $O$ . A particle  $P$  of mass  $4M$  is attached to the other end of the string and hangs vertically in equilibrium. Another particle of mass  $2M$  is attached to  $P$  and the combined particle is then released from rest. The speed of the combined particle when it has descended a distance  $\frac{1}{4}a$  is  $v$ .

Find an expression for  $v$  in terms of  $g$  and  $a$ .

[6]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dotted lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, leaving ample room for practicing various letters and words. There is no text or other markings on the page.



- 4 A particle  $P$  of mass  $5\text{ kg}$  moves along a horizontal straight line. At time  $t\text{ s}$ , the velocity of  $P$  is  $v\text{ m s}^{-1}$  and its displacement from a fixed point  $O$  on the line is  $x\text{ m}$ . The forces acting on  $P$  are a force of magnitude  $\frac{500}{v}\text{ N}$  in the direction  $OP$  and a resistive force of magnitude  $\frac{1}{2}v^2\text{ N}$ . When  $t = 0$ ,  $x = 0$  and  $v = 5$ .

(a) Find an expression for  $v$  in terms of  $x$ .

[6]

This image shows a full page of a worksheet designed for handwriting practice. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for letter height. The entire page is otherwise blank, with no margins, text, or other markings.

(b) State the value that the speed approaches for large values of  $x$ .

[1]

- 5 A particle  $P$  is projected with speed  $u \text{ ms}^{-1}$  at an angle of  $\theta$  above the horizontal from a point  $O$  on a horizontal plane and moves freely under gravity. The horizontal and vertical displacements of  $P$  from  $O$  at a subsequent time  $t$  s are denoted by  $x$  m and  $y$  m respectively.

(a) Show that the equation of the trajectory is given by

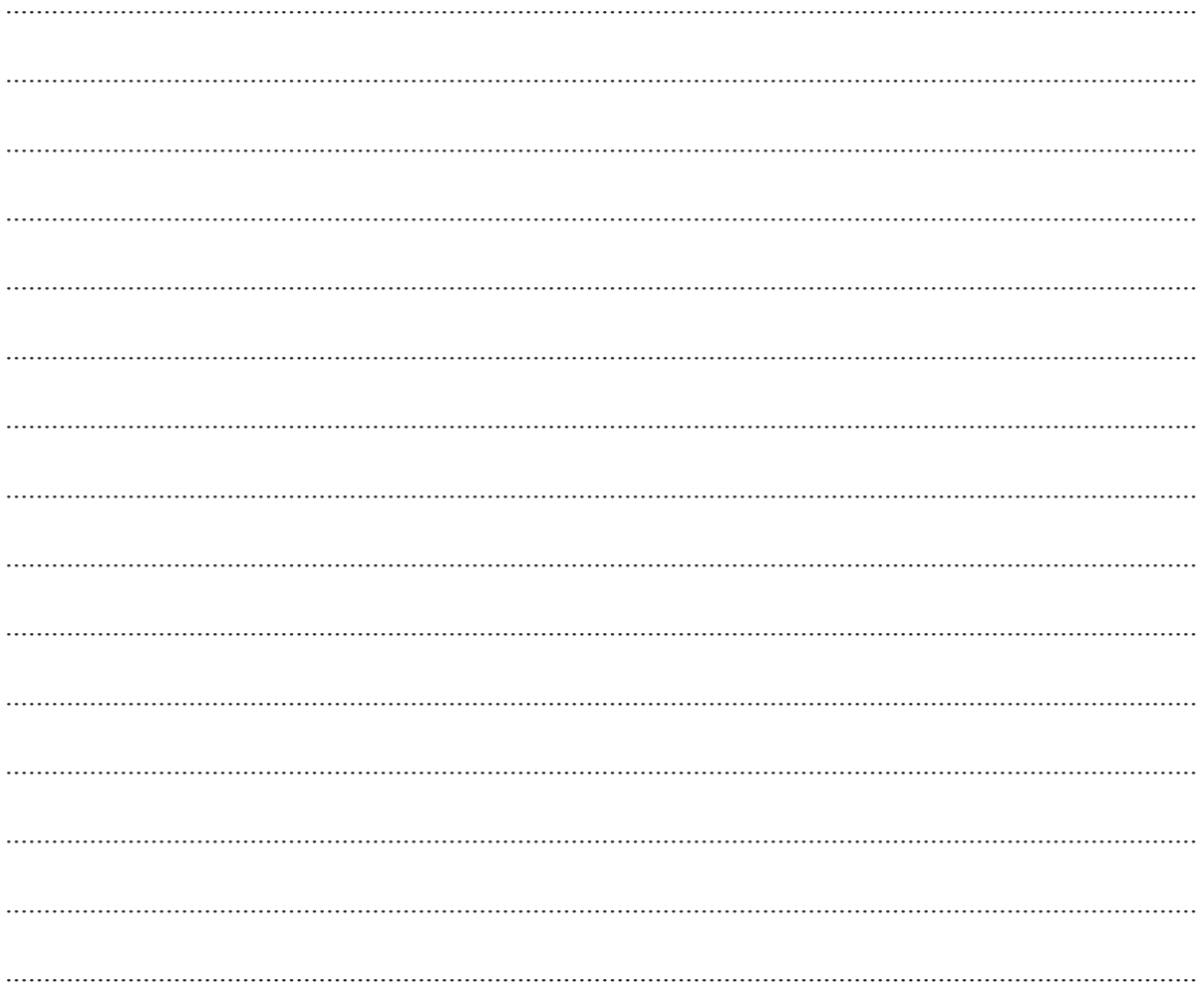
$$y = x \tan \theta - \frac{gx^2}{2u^2}(1 + \tan^2 \theta). \quad [4]$$

[illegible]

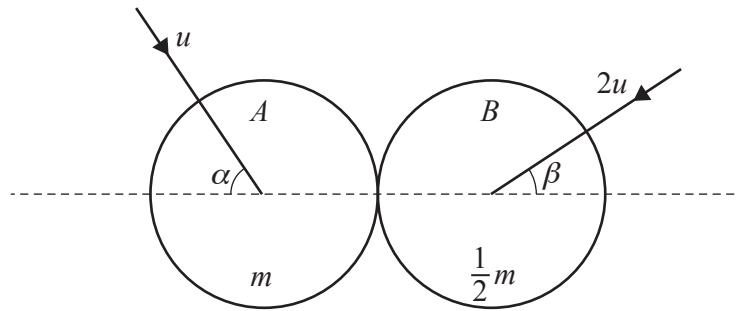
In the subsequent motion  $P$  passes through the point with coordinates  $(30, 20)$ .

- (b)** Given that one possible value of  $\tan \theta$  is  $\frac{4}{3}$ , find the other possible value of  $\tan \theta$ . [5]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.



[illegible]



Two uniform smooth spheres  $A$  and  $B$  of equal radii have masses  $m$  and  $\frac{1}{2}m$  respectively. The two spheres are moving on a horizontal surface when they collide. Immediately before the collision, sphere  $A$  is travelling with speed  $u$  and its direction of motion makes an angle  $\alpha$  with the line of centres. Sphere  $B$  is travelling with speed  $2u$  and its direction of motion makes an angle  $\beta$  with the line of centres (see diagram). The coefficient of restitution between the spheres is  $\frac{5}{8}$  and  $\alpha + \beta = 90^\circ$ .

- (a) Find the component of the velocity of  $B$  parallel to the line of centres after the collision, giving your answer in terms of  $u$  and  $\alpha$ . [4]

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

The direction of motion of  $B$  after the collision is parallel to the direction of motion of  $A$  before the collision.

**(b)** Find the value of  $\tan \alpha$ .

[5]

This image shows a full page of a handwriting practice worksheet. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for letter height. The lines are evenly spaced across the entire page, providing a guide for consistent letter formation. There is no text or other markings on the page.

## Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.

[illegible]



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