

Cambridge International AS & A Level

CANDIDATE
NAME

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MATHEMATICS

9709/62

Paper 6 Probability & Statistics 2

February/March 2022

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages.

- 1** The lengths, in millimetres, of a random sample of 12 rods made by a certain machine are as follows.

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- (a)** Find unbiased estimates of the population mean and variance. [3]

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- (b)** Give a statistical reason why these estimates may not be reliable. [1]

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- 2 Harry has a five-sided spinner with sectors coloured blue, green, red, yellow and black. Harry thinks the spinner may be biased. He plans to carry out a hypothesis test with the following hypotheses.

$$H_0: P(\text{the spinner lands on blue}) = \frac{1}{5}$$

$$H_1: P(\text{the spinner lands on blue}) \neq \frac{1}{5}$$

Harry spins the spinner 300 times. It lands on blue on 45 spins.

Use a suitable approximation to carry out Harry's test at the 5% significance level.

[5]

This image shows a full page of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page, providing a template for handwriting practice or general writing. There are no margins, text, or other markings on the page.

- 3 A random sample of 500 households in a certain town was chosen. Using this sample, a confidence interval for the proportion, p , of all households in that town that owned two or more cars was found to be $0.355 < p < 0.445$.

Find the confidence level of this confidence interval. Give your answer correct to the nearest integer.

[5]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting or typing. There are no margins, text, or other markings on the page.

- (a) Assuming that the standard deviation of the time for the new challenge is 5.2 minutes, test at the 1% significance level whether the population mean time for the new challenge is less than 25.5 minutes. [5]

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

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5 The heights of buildings in a large city are normally distributed with mean 18.3 m and standard deviation 2.5 m.

- (a) Find the probability that the total height of 5 randomly chosen buildings in the city is more than 95 m. [4]

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- (b) Find the probability that the difference between the heights of two randomly chosen buildings in the city is less than 1 m. [5]

This image shows a full page of white paper with horizontal dotted lines, typical of primary school writing paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- 6** In a game a ball is rolled down a slope and along a track until it stops. The distance, in metres, travelled by the ball is modelled by the random variable X with probability density function

$$f(x) = \begin{cases} -k(x-1)(x-3) & 1 \leq x \leq 3, \\ 0 & \text{otherwise,} \end{cases}$$

where k is a constant.

- (a)** Without calculation, explain why $E(X) = 2$. [1]

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- (b)** Show that $k = \frac{3}{4}$. [3]

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(c) Find $\text{Var}(X)$.

[3]

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One turn consists of rolling the ball 3 times and noting the largest value of X obtained. If this largest value is greater than 2.5, the player scores a point.

(d) Find the probability that on a particular turn the player scores a point.

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- 7 (a) Two ponds, A and B , each contain a large number of fish. It is known that 2.4% of fish in pond A are carp and 1.8% of fish in pond B are carp. Random samples of 50 fish from pond A and 60 fish from pond B are selected.

Use appropriate Poisson approximations to find the following probabilities.

- (i) The samples contain at least 2 carp from pond A and at least 2 carp from pond B . [3]

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- (ii) The samples contain at least 4 carp altogether. [3]

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- (b) The random variables X and Y have the distributions $\text{Po}(\lambda)$ and $\text{Po}(\mu)$ respectively. It is given that
- $P(X = 0) = [P(Y = 0)]^2$,
 - $P(X = 2) = k[P(Y = 1)]^2$, where k is a non-zero constant.

Find the value of k .

[4]

[illegible]

[illegible]

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