

Cambridge International AS & A Level

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MATHEMATICS

9709/21

Paper 2 Pure Mathematics 2

May/June 2023

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **12** pages.

- 1 Use logarithms to solve the equation $12^x = 3^{2x+1}$. Give your answer correct to 3 significant figures. [4]

[illegible]

- 2** A curve has equation $y = \frac{2 + 3 \ln x}{1 + 2x}$.

Find the equation of the tangent to the curve at the point $(1, \frac{2}{3})$. Give your answer in the form $ax + by + c = 0$, where a , b and c are integers. [5]

[illegible]

3 It is given that $\int_0^a (3e^{2x} - 1) dx = 12$, where a is a positive constant.

(a) Show that $a = \frac{1}{2} \ln(9 + \frac{2}{3}a)$. [4]

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(b) Use an iterative formula, based on the equation in (a), to find the value of a correct to 4 significant figures. Use an initial value of 1 and give the result of each iteration to 6 significant figures. [3]

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- 4 The polynomial $p(x)$ is defined by

$$p(x) = 2x^3 + 3x^2 + kx - 30,$$

where k is a constant. It is given that $(x - 3)$ is a factor of $p(x)$.

- (a) Find the value of k . [2]

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- (b) Hence find the quotient when $p(x)$ is divided by $(x - 3)$ and factorise $p(x)$ completely. [3]

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- (c) It is given that a is one of the roots of the equation $p(x) = 0$.

Given also that the equation $|4y - 5| = a$ is satisfied by two real values of y , find these two values of y . [3]

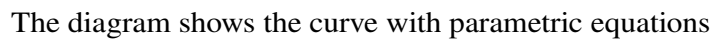
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for $-\frac{1}{4}\pi \leq t \leq \frac{1}{4}\pi$. The curve has a maximum point M .

- [illegible]

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6 Show that $\int_{\frac{1}{4}\pi}^{\frac{1}{3}\pi} \left(4 \cos^2 2x + \frac{1}{\cos^2 x} \right) dx = \frac{3}{4}\sqrt{3} + \frac{1}{6}\pi - 1.$ [7]

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- 7 (a) Express $7 \cos \theta + 24 \sin \theta$ in the form $R \cos(\theta - \alpha)$, where $R > 0$ and $0^\circ < \alpha < 90^\circ$. Give the value of α correct to 2 decimal places. [3]

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- (b) Solve the equation $7 \cos \theta + 24 \sin \theta = 18$ for $0^\circ < \theta < 360^\circ$. [4]

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$$\frac{150}{7 \cos \frac{1}{2}\beta + 24 \sin \frac{1}{2}\beta + 50}$$

is denoted by V .

Find the value of V and determine the smallest positive value of β (in degrees) for which the value of V occurs. [4]

[illegible]

[illegible]

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