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**Cambridge International Advanced Subsidiary Level**

# MARK SCHEME for the October/November 2014 series

## 9709 MATHEMATICS

**9709/22** Paper 2, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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**Mark Scheme Notes**

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

**Penalties**

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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**1** Either: Square both sides obtaining 3 terms on each side — M1
Solve 3-term quadratic equation — M1
Obtain $-\frac{4}{5}$ and 6 — A1 [3]
Or: Obtain value 6 from graphical method, inspection, linear equation, … — B1
Obtain value $-\frac{4}{5}$ similarly — B2 [3]

**2** **(i)** Integrate to obtain form $pe^{-x}+qe^{-3x}$ where $p\neq 1, q\neq 6$ — M1
Obtain $-e^{-x}-2e^{-3x}$ (allow unsimplified) — A1
Apply both limits to $pe^{-x}+qe^{-3x}$ (allow $p=1, q=6$) — M1
Obtain $3-e^{-a}-2e^{-3a}$ — A1 [4]

**(ii)** State 3 following a result of the form $k+pe^{-x}+qe^{-3x}$ — B1√ [1]

**3** Obtain $6y+6x\frac{dy}{dx}$ as derivative of $6xy$ — B1
Obtain $2y\frac{dy}{dx}$ as derivative of $y^2$ — B1
Obtain $\frac{3}{x}$ and $\frac{d}{dx}(16)=0$ — B1
Substitute 1 and 2 to find value of $\frac{dy}{dx}$ — M1
Obtain value $\frac{2}{3}$ as gradient of normal following their value of $\frac{dy}{dx}$ — A1√
Form equation of **normal** through (1, 2) with numerical gradient — M1
Obtain $2x-3y+4=0$ — A1 [7]

**4** **(a)** Use power law to produce $\ln(x-4)^2$ — B1
Apply logarithm laws to produce equation without logarithms — M1
Obtain $(x-4)^2=2x$ or equivalent — A1
Solve 3-term quadratic equation — DM1
Obtain (finally) $x=8$ only — A1 [5]

**(b)** Apply logarithms and use power law (once) — M1
Obtain $\frac{\ln 10^{10}}{\ln 1.4}$ or equivalent as part of inequality or equation — A1
Conclude with single integer 69 — A1 [3]

**5** **(i)** Differentiate to obtain $-2\sin x+2\sin 2x$ or equivalent — B1
Use $\sin 2x=2\sin x\cos x$ or equivalent — B1
Equate first derivative to zero and solve for $x$ — M1
Obtain $\frac{1}{3}\pi$ — A1 [4]

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| | **(ii)** | Integrate to obtain form $k_1 \sin x + k_2 \sin 2x$ | M1 | |
| | | Obtain correct $2\sin x - \frac{1}{2}\sin 2x$ | A1 | |
| | | Apply limits 0 and their answer from part **(i)** | M1 | |
| | | Obtain $\frac{3}{4}\sqrt{3}$ or exact equivalent | A1 | [4] |
| **6** | **(i)** | Identify $x-3$ as divisor | B1 | |
| | | Divide by linear expression at least as far as $x$ term | M1 | |
| | | Obtain quotient $x^3 + 3x - 16$ | A1 | |
| | | Obtain zero remainder with no errors in the division | A1 | |
| | | Equate quotient to zero and confirm $x = \sqrt[3]{16 - 3x}$ (AG) | A1 | [5] |
| | **(ii)** | Use iteration process correctly at least once | M1 | |
| | | Obtain final answer 2.13 | A1 | |
| | | Show sufficient iterations to 4 decimal places or show a sign change in the interval (2.125, 2.135) | A1 | [3] |
| **7** | **(i)** | State or imply $R = 13$ | B1 | |
| | | Use appropriate formula to find $\alpha$ | M1 | |
| | | Obtain 67.38° | A1 | [3] |
| | **(ii)** | Attempt to find at least one value of $\cos^{-1}\frac{8}{13}$ or $\cos^{-1}\frac{8}{R}$ | M1 | |
| | | Obtain one correct value of $\theta$ (240.6 or 344.6) | A1 | |
| | | Carry out correct method to find second value of $\theta$ within the range | DM1 | |
| | | Obtain second correct value (344.6 or 240.6) | A1 | [4] |
| | **(iii)** | State or imply $7 + 13\cos\left(\frac{1}{2}\phi + 67.38\right)$ following their answers from part **(i)** | B1√ | |
| | | State 20 | B1 | |
| | | Attempt to find $\phi$ for which $\cos\left(\frac{1}{2}\phi + 67.38\right) = 1$ | M1 | |
| | | Obtain 585.2 | A1 | [4] |

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