

CANDIDATE
NAME

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MATHEMATICS

9709/13

Paper 1 Pure Mathematics 1 (P1)

October/November 2017

1 hour 45 minutes

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.

- 1** An arithmetic progression has first term -12 and common difference 6 . The sum of the first n terms exceeds 3000 . Calculate the least possible value of n . [4]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

- 2** Find the set of values of a for which the curve $y = -\frac{2}{x}$ and the straight line $y = ax + 3a$ meet at two distinct points. [4]

[illegible]

- 3 (i) Find the term independent of x in the expansion of $\left(\frac{2}{x} - 3x\right)^6$. [2]

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- (ii) Find the value of a for which there is no term independent of x in the expansion of

$$(1 + ax^2)\left(\frac{2}{x} - 3x\right)^6. \quad [3]$$

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- 4 The function f is such that $f(x) = (2x - 1)^{\frac{3}{2}} - 6x$ for $\frac{1}{2} < x < k$, where k is a constant. Find the largest value of k for which f is a decreasing function. [5]

[illegible]

5 (i) Show that the equation $\frac{\cos \theta + 4}{\sin \theta + 1} + 5 \sin \theta - 5 = 0$ may be expressed as $5 \cos^2 \theta - \cos \theta - 4 = 0$. [3]

[illegible]

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6 The functions f and g are defined by

$$\begin{aligned} f(x) &= \frac{2}{x^2 - 1} \text{ for } x < -1, \\ g(x) &= x^2 + 1 \text{ for } x > 0. \end{aligned}$$

(i) Find an expression for $f^{-1}(x)$.

[3]

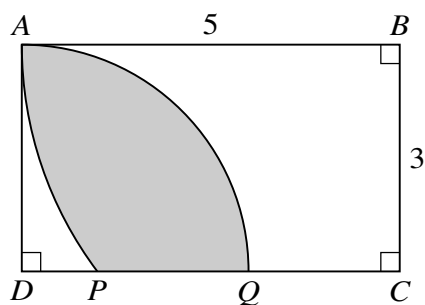
[illegible]

(ii) Solve the equation $gf(x) = 5$.

[4]

[illegible]

7



The diagram shows a rectangle $ABCD$ in which $AB = 5$ units and $BC = 3$ units. Point P lies on DC and AP is an arc of a circle with centre B . Point Q lies on DC and AQ is an arc of a circle with centre D .

- (i) Show that angle $ABP = 0.6435$ radians, correct to 4 decimal places. [1]

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- (ii) Calculate the areas of the sectors BAP and DAQ . [3]

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(iii) Calculate the area of the shaded region.

[3]

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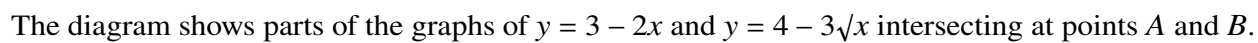
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- This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, which is otherwise blank.

[illegible]

$$\overrightarrow{OA} = \begin{pmatrix} 8 \\ -6 \\ 5 \end{pmatrix}, \quad \overrightarrow{OB} = \begin{pmatrix} -10 \\ 3 \\ -13 \end{pmatrix} \quad \text{and} \quad \overrightarrow{OC} = \begin{pmatrix} 2 \\ -3 \\ -1 \end{pmatrix}.$$

(i) Find the magnitudes $|\vec{AB}|$, $|\vec{BC}|$ and $|\vec{CD}|$. [5]

[illegible]

- (ii) Given that D is a point lying on the line through B and C , find the two possible position vectors of the point D . [4]

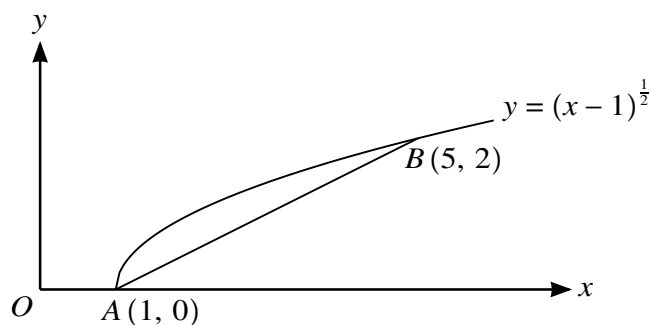
[illegible]

- (i) Find, in terms of a and b , the non-zero value of x for which the curve has a stationary point and determine, showing all necessary working, the nature of the stationary point. [3]

[illegible]

- (ii)** It is now given that the curve has a stationary point at $(-2, -3)$ and that the gradient of the curve at $x = 1$ is 9. Find $f(x)$. [6]

[illegible]



The diagram shows the curve $y = (x - 1)^{\frac{1}{2}}$ and points $A(1, 0)$ and $B(5, 2)$ lying on the curve.

- (i) Find the equation of the line AB , giving your answer in the form $y = mx + c$. [2]

- (ii) Find, showing all necessary working, the equation of the tangent to the curve which is parallel to AB . [5]

This image shows a full page of white paper with ten horizontal dashed lines, typical of primary school handwriting practice paper. The lines are evenly spaced and extend across the entire width of the page. There is no text or other markings on the paper.

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- (iii) Find the perpendicular distance between the line AB and the tangent parallel to AB . Give your answer correct to 2 decimal places. [3]

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